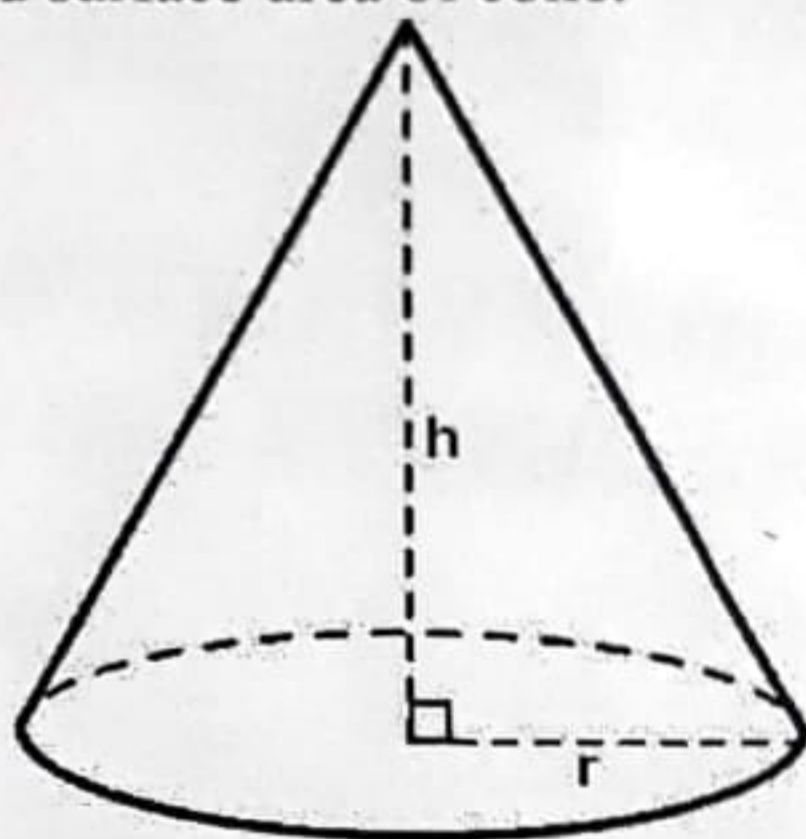


Questions based on,

- Electric field and electrostatic potential
- Electrostatic energy of system of charges
- Capacitance of a system of charged conductors
- Method of images

- [1] A charge 'q' is placed at the centre of the base of a cone as shown in the diagram. Find the electric flux through the curved surface area of cone.



- [2] A point charge 'q' is located at the centre of a cube having edge of length 'd'. What is the value of flux over one face of the cube? If the charge is placed at one corner of the cube, then what will be the value of electric flux through each face of the cube?

- [3] A spherical charge distribution has a volume charge density $\rho(r)$ given by,

$$\rho(r) = \begin{cases} \rho_0 \left(1 - \frac{5r^2}{R^2}\right) & r \leq R \\ 0 & r > R \end{cases}$$

Calculate the electric field at points, $r < R$ and $r > R$.

- [4] Calculate the electric field intensity due to a spherical charge distribution which is given by,

$$\rho(r) = \begin{cases} \rho_0 \left(1 - \frac{r}{R}\right) & r < R \\ 0 & r > R \end{cases}$$

Find the value of 'r' at which the electric field is maximum.

- [5] Find the electric field at the centre of,
- A uniformly charged semicircular arc.
 - A hemisphere which is charged uniformly with a surface density σ .

- [6] A finite sheet lies on the $z = 0$ plane, such that $0 \leq x \leq 1\text{m}$ and $0 \leq y \leq 1\text{m}$. It has a charge density given by,

$$\sigma = axy(x^2 + y^2 + 25\text{m}^2)^{3/2} \text{ nC/m}^2$$

Here, a is a constant with appropriate units. Find the total charge on the sheet and the electric field at $(0,0,5\text{m})$.

- [7] If the electric field is given by $\vec{E} = a[8\hat{i} + 4\hat{j} + 3\hat{k}]$ N/C, then calculate the electric flux through a surface of area 100 m^2 lying in the $x - y$ plane. Here, a is a constant with appropriate units.
- [8] Find the potential on the axis of a uniformly charged cylinder, a distance ' z ' from the centre. It is given that the length of the cylinder is L , its radius is r and the charge density is ρ . Use your result to find the electric field at this point. (Assume that $z > L/2$).
- [9] Show that the electric is zero at all points inside a conductor having static charge. Also show that the electric field is normal to the surface of such conductor at every point.
- [10] An inverted hemispherical bowl of radius R carries a uniform surface charge density. Find the potential difference between North Pole and centre.
- [11] A solid conducting sphere is concentric with a thin conducting shell. The inner sphere carries a charge Q_1 , and the spherical shell carries a charge Q_2 , such that $Q_2 = -3Q_1$.
- How is the charge distributed on the sphere?
 - Calculate the charge densities distributed on the spherical shell (inner and outer surface of the shell)?
 - What is the electric field at $r < R_1$, between R_1 and R_2 , at $r > R_2$?
 - What happens when you connect the two spheres with a wire?
- [12] An isolated conductor of arbitrary shape has a net charge of $10\mu\text{C}$. There is a cavity inside the conductor within which there is a point charge of $3\mu\text{C}$.
- What is the charge on the cavity wall?
 - What is the charge on the outer surface of the conductor?
- [13] Consider a charged sphere of radius R containing charge q , completely enclosed by a spherical cavity of inner radius ' a ' and outer radius ' b '. Calculate the charge density on all surfaces and potential everywhere.
- [14] A copper sphere of radius 4 cm carries a uniformly distributed total charge of $5\mu\text{C}$ on its surface in face space.
- Use Gauss's law to find electric flux density vector D external to the sphere.
 - Calculate the total energy stored in the electrostatic field.
 - Calculate the capacitance of the isolated sphere.
- [15] A point charge ' q ' is placed inside a hollow grounded, conducting sphere of inner radius ' a '. Using the method of images,
- Find the potential inside the sphere
 - Find the induced surface-charge density.
- [16] Three identical point charges of 4 pC each are located at the corners of equilateral triangle having each side of 0.5 mm. How much work must be done to move one charge to a point equidistant from the other two and on the line joining them?

[17] Two spherical cavities, of radii 'a' and 'b', are hollowed out from the interior of a neutral conducting sphere of radius R. At the center of each cavity point charge q_a and q_b are placed respectively.

- Find the surface charges densities σ_a, σ_b and σ_R .
- What is the field outside the conductor?
- What is the field outside the conductor and within each cavity?
- What is the force on q_a and q_b ?

Questions based on,

- Dielectric Properties of Matter
- Capacitor filled with dielectric
- Gauss law in dielectrics

Type-B

[1] In a parallel plate air capacitor having plate separation 0.04 mm, an electric field of 4×10^4 V/m is established between the plates. The battery is then removed and a metal plate of thickness 0.03 mm is inserted between the plates of the capacitor. Determine the potential difference across the capacitor,

- Before the introduction of metal plates
- After the introduction of metal plates
- If dielectric slab with dielectric constant 2.5 and same thickness is inserted instead of the metal plates

[2] The space between the plates of a parallel plate capacitor (kept at 'd' distance apart and each having area A) is filled with a dielectric, whose relative permittivity varies according with distance (x) according to the relation,

$$\epsilon_r = \frac{1}{1 + \frac{x^2}{d^2}}$$

Find the capacitance of the capacitor.

[3] An isolated conducting sphere of radius 'a' is enclosed within an earthed concentric sphere of radius 'b'. Show that capacitance of this system will be 'n' times that of an isolated sphere, if

$$\frac{b}{a} = \frac{n}{n-1}$$

[4] A $4 \mu F$ capacitor has a charge of $40 \mu C$ and a $3 \mu F$ capacitor has a charge of $10 \mu C$. The negative plate of each one is connected to the positive plate of the other. Determine,

- The charge on each capacitor
- The potential difference across each capacitor

[5] A $4 \mu F$ capacitor has a charge of $40 \mu C$ and a $3 \mu F$ capacitor has a charge of $10 \mu C$. The capacitors are connected such that plates of like charge are connected together. Determine,

- The initial potential difference across each capacitor
- The final potential difference across each capacitor

- c) The initial energy of each capacitor
- d) The final energy of the combination
- e) The energy lost in connecting them together.

Questions based on,

- Magnetic Field
- Biot-Savart Law and its applications
- Ampere's Circuital Law and its application
- Vector Potential
- Magnetic Properties of Matter

Type - C

- [1] A current I flows down a wire of radius R .
- a) If it is uniformly distributed over the surface, what will be the current density?
 - b) If it is distributed in such a way that the volume current density is inversely proportional to the distance from the axis, then what will be the current density?
- [2] Consider three straight, infinitely long, equally spaced wires (zero radius), each carrying a current I in the same direction.
- a) Calculate the location of points of zero magnetic field.
 - b) Sketch the magnetic field pattern.
- [3] Two coaxial solenoids are each carrying a current I , but in opposite directions. The inner solenoid of radius ' a ' has N_1 turns per unit length and the outer solenoid of radius ' b ' has N_2 turns per unit length. Find \mathbf{B} in each of the three regions,
- a) Inside the inner solenoid
 - b) Between the solenoids
 - c) Outside both the solenoids
- [4] An infinite solenoid having N turns per unit length and current ' I ' is filled with a linear magnetic material.
- a) Find the magnetic field inside the solenoid.
 - b) Find the bound surface current density.
 - c) Explain what will be the difference in the field found above, if the magnetic material is paramagnetic or diamagnetic.
- [5] Consider a large parallel plate capacitor with uniform surface charge density σ on the upper plate and $-\sigma$ on the lower plate. Both the plates are together moving towards right with a constant speed v . Find the magnetic field between, above and below the two plates of the capacitor.
- [6] At the equator, the strength of the earth's magnetic field is $\sim 0.03 \text{ mWb/m}^2$. If a piece of copper wire 1 m long and cross-sectional area $3 \times 10^{-6} \text{ m}^2$ is to be kept afloat in a horizontal position perpendicular to the direction of the magnetic field, how much current needs to be passed through the wire. Given that density of copper is $9 \times 10^3 \text{ kg/m}^3$

[7] An electron moving speed $v = 3 \times 10^6$ m/s enters the gap between the plates of a parallel plate capacitor, midway between the plates with its velocity parallel to the plates. The plates are separated by a distance of 1cm, the potential difference between the plates is 100 V and the length of the plates is 30 cm. A fluorescent screen is placed at a distance D from the further end of the plates. Determine the distance from the midpoint of the screen where the electron will hit. Assume that the field is non zero only between the plates and neglect edge effects.

[8] A very thin disc of radius R , carrying a uniform surface charge density σ lies parallel to the $x - y$ plane. It rotates about the z -axis (passing through its center) with an angular speed ω . Find the direction and magnitude of the magnetic field at the center of the disk.

[9] A circular current carrying coil of radius R is in the $x - y$ plane with its centre at $z = 0$. The magnetic field at point P on the z -axis at a distance ' z ' above the centre is well known. Using the expression and the fact that $\vec{\nabla} \cdot \vec{B} = 0$, obtain the value of B_x and B_y at a point Q away from the axis the same value of z as P but removed by small values of x and y . Retain terms only up to first order in x and y .

Questions based on,

- Electromagnetic Induction
- Self Inductance and Mutual Inductance
- Charge Conservation and Displacement current

Type - D

[1] A 50 cm long wire is moved in the y -direction at a speed of 25 m/sec, so that the wire is always parallel to the x -axis. The components of the magnetic field are,

$$B_x = 0.2 \text{ Wb/m}^2$$

$$B_y = -0.4 \text{ Wb/m}^2$$

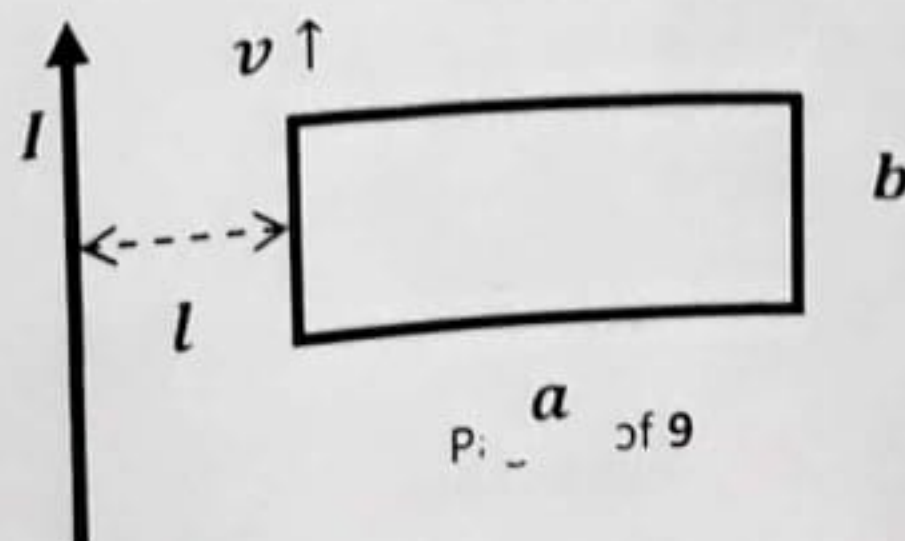
$$B_z = 0.3 \text{ Wb/m}^2$$

Find the e.m.f induced in the wire.

[2] A long cylindrical solenoid with 50 loops per 1 cm has a radius of 1.5 cm. Assume that the magnetic field inside the solenoid is homogeneous and parallel to the axis of the solenoid.

- a) What is the inductance of the solenoid per 1 meter of its length?
- b) What is the induced electromotive force per 1 meter of the length of solenoid if the current is changing at a rate of 10 A/s?

[3] A current I flows through a long straight filamentary wire. A conducting rectangular loop, of side, a , and b , is placed at a distance l from the wire. The loop moves with a velocity v in the direction as shown in diagram. Calculate the magnitude of e.m.f induced in the loop after a time t .



[4] A small circular loop, of radius r , is kept parallel to a big circular loop, of radius, R ($R \gg r$), such that its center is along the axis of the big loop. Distance between the centers of the two loops is d . Determine the coefficient of mutual inductance, due to a current, I , flowing through the loops.

[5] Show that the total magnetic energy associated with a pair of coupled circuits varying currents I_1 and I_2 is given by,

$$U = \frac{1}{2}L_1I_1^2 + \frac{1}{2}L_2I_2^2 \pm MI_1I_2$$

[6] Assuming sea water has $\mu = \mu_0$, $\epsilon = 81\epsilon_0$, $\sigma = 20 \text{ S/m}$, determine the frequency at which magnitude of conduction current density is 5 times that of the displacement current density.

[7] Demonstrate that the law of electric charge conservation ($\vec{\nabla} \cdot \vec{j} = -\frac{\partial \rho}{\partial t}$) follows from the Maxwell's equations.

Questions based on,

- Electrical Circuits
- Series and parallel LCR Circuit
- Network theorems
- Mesh & Node Analysis

Type-E

[1] What is the value of internal resistance of a constant voltage source?

[2] Why can an ideal constant current source not be constructed?

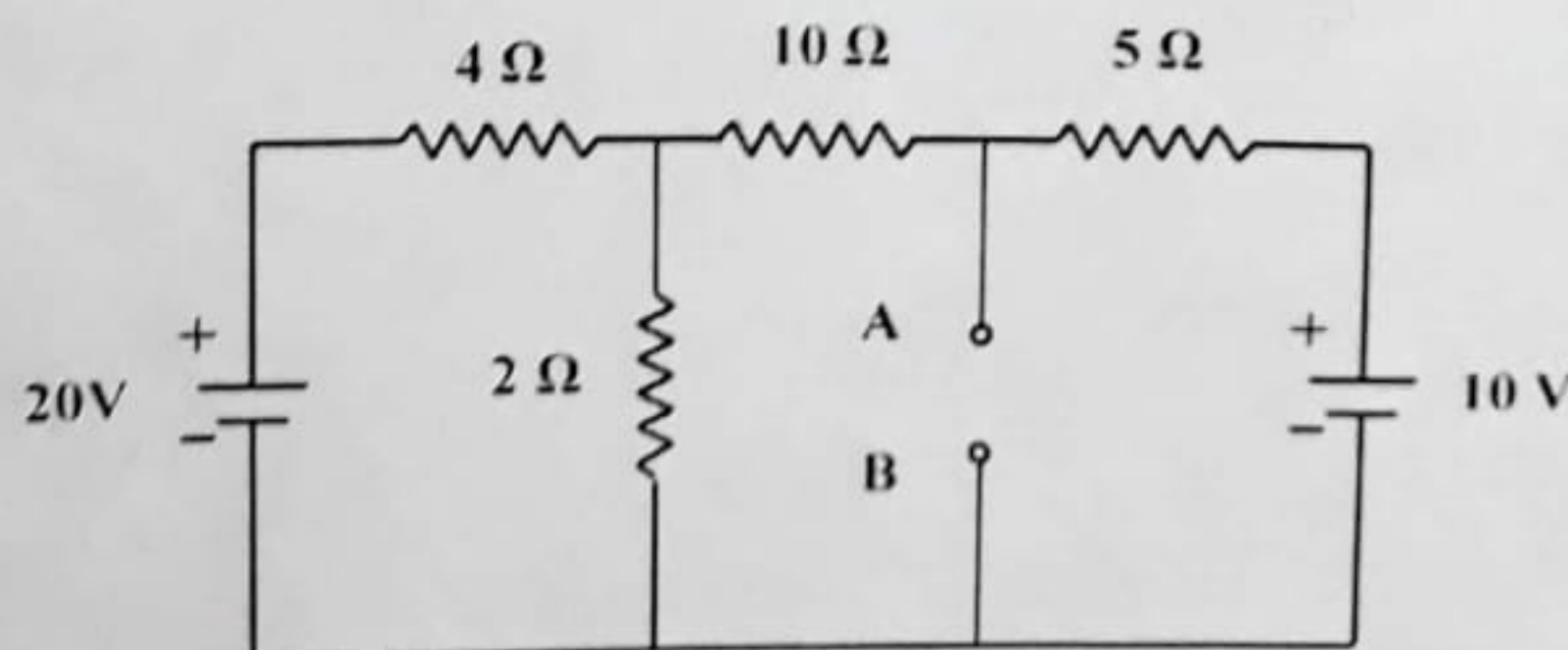
[3] A series LCR circuit with $L = 25 \text{ nH}$, $C = 70 \mu\text{F}$ has a lagging phase angle of 20° at $\omega = 2 \text{ kHz}$. At what frequency will the phase angle be leading 30° ?

[4] A series LCR circuit has $R = 4 \Omega$, $L = 0.5 \text{ H}$, $V = 100 \cos 50\pi t$. Find the value of C for resonance. Also determine the voltage across C .

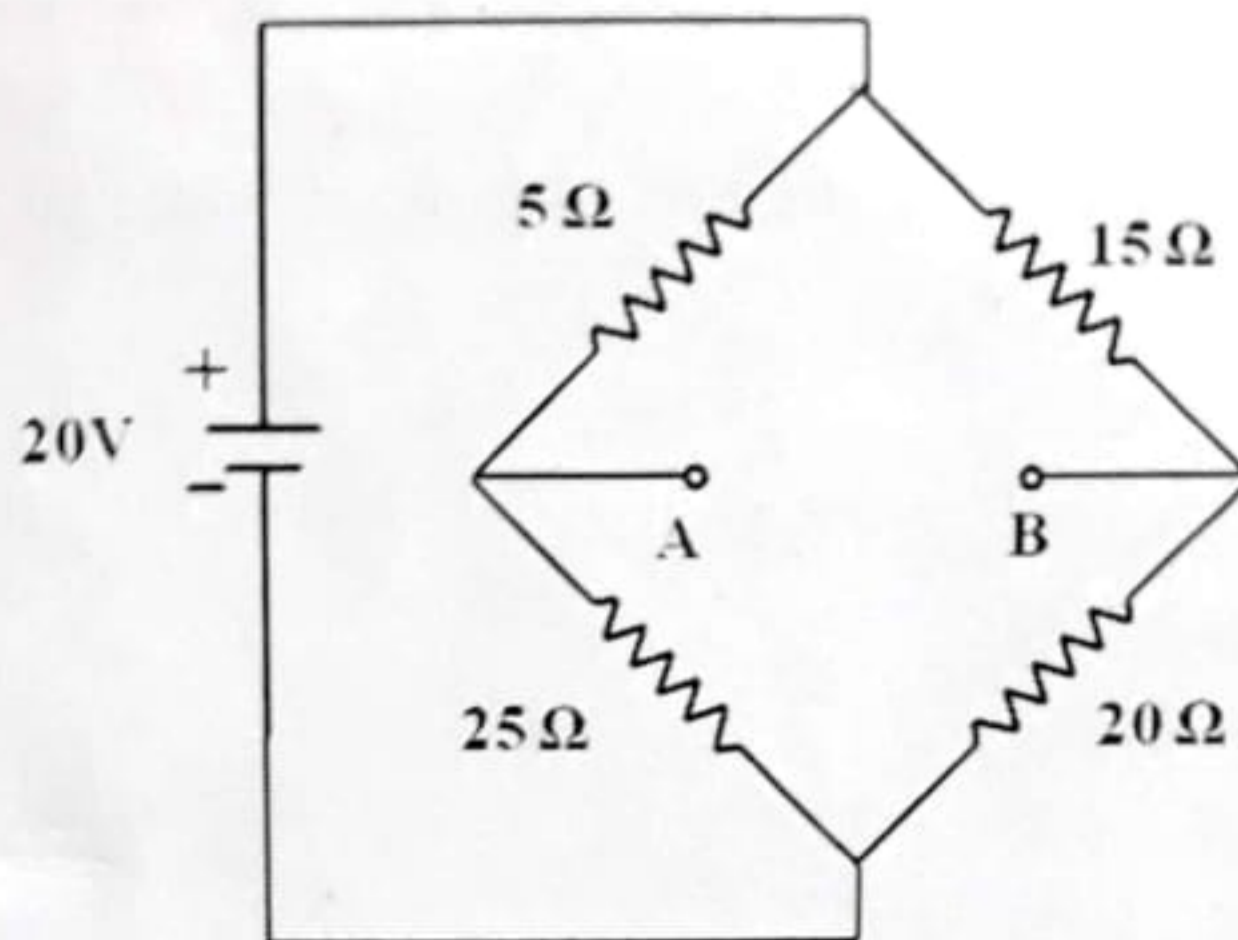
[5] Plot the variation of quality factor with resistance for a series LCR circuit.

[6] Obtain the Thevenin's equivalent circuit for the following circuits,

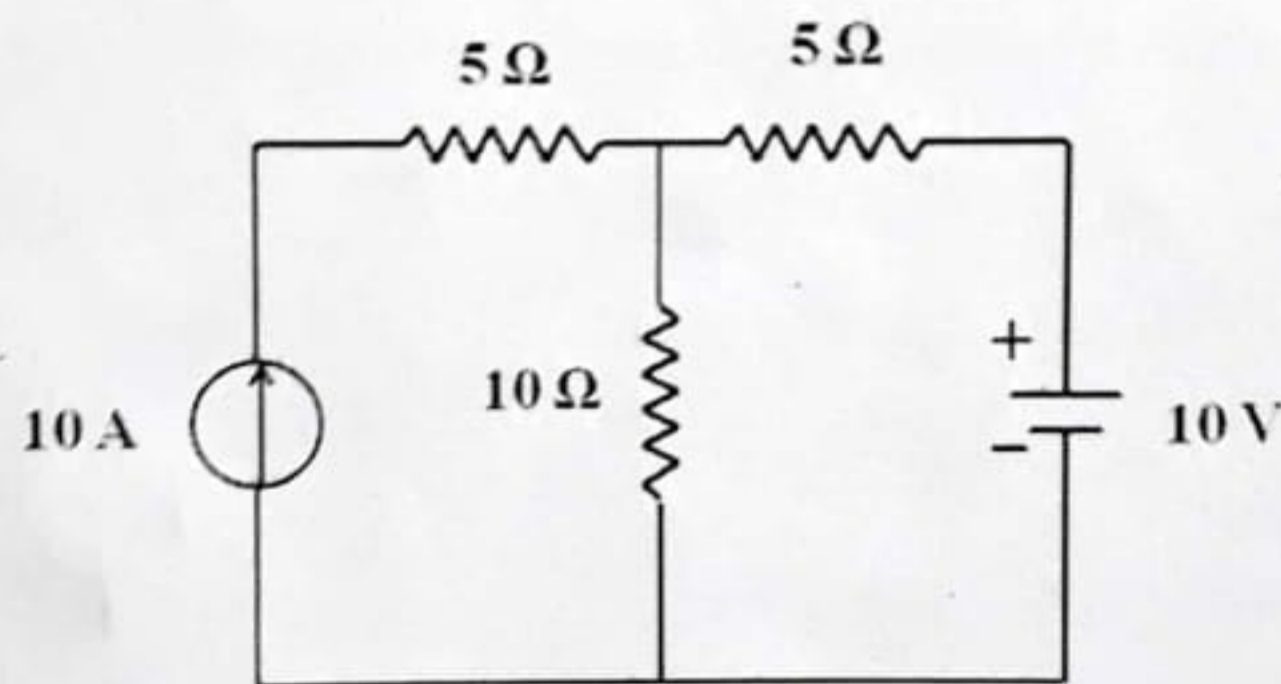
(i)



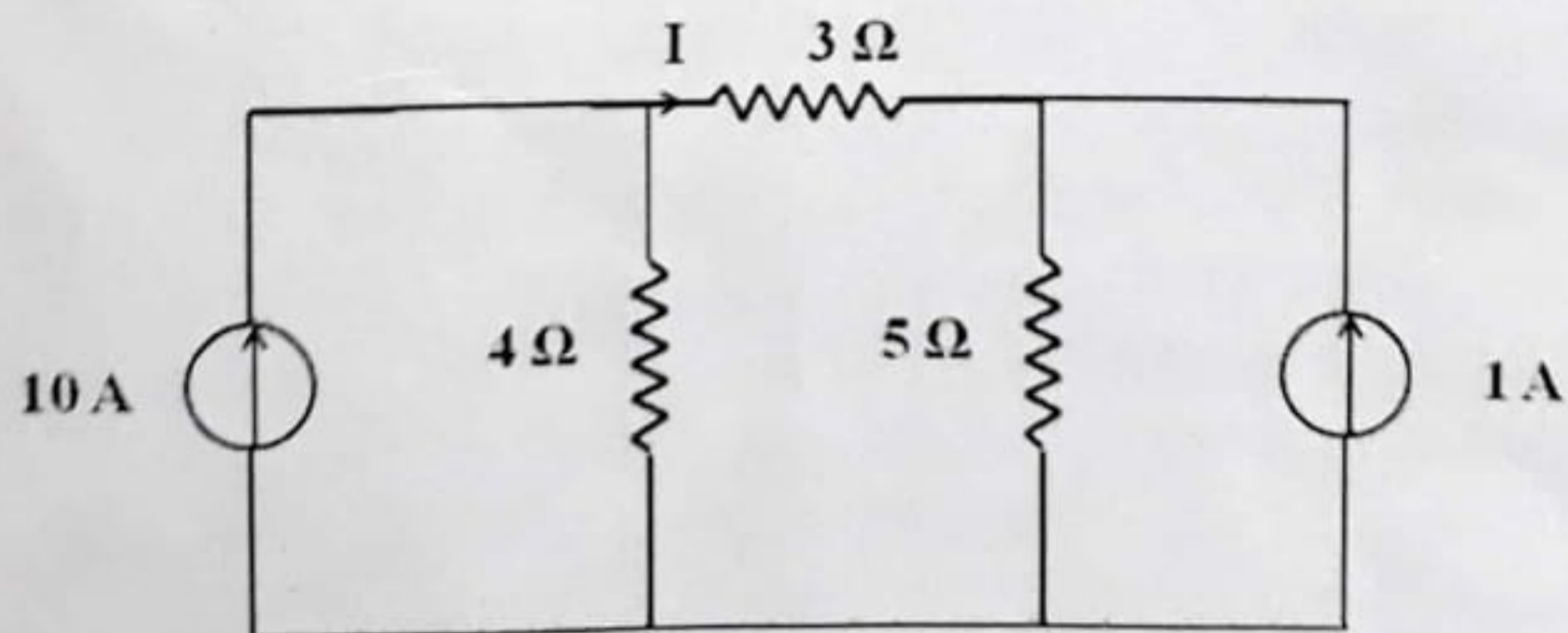
(ii)



[7] Find the current flowing through the $10\ \Omega$ resistance in the following circuit.



[8] For the following circuit, find the current I using the Norton's theorem.



[9] In the following circuit, the total power dissipated is 64 W. Calculate the value of the resistance R .

